

# Slicing of Extended Finite State Machines

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Mark Harman<sup>1</sup>, Rob Hierons<sup>2</sup>, Zheng Li<sup>1</sup> and Laurence Tratt<sup>3</sup>



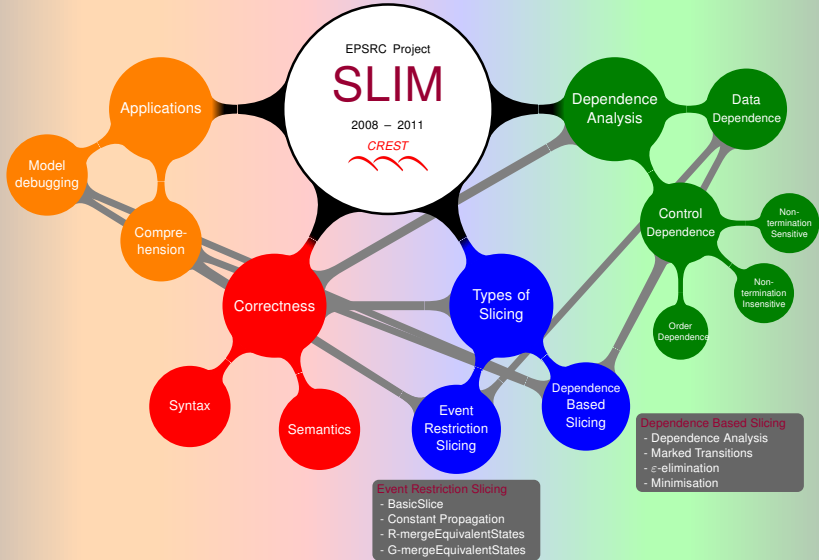
**Centre for Research in Evolution,  
Search & Testing**

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<sup>2</sup>Brunel University

<sup>3</sup>Bournemouth University

# Slicing state based Models



**Benchmarks**

- ATM
- Cashier
- CruiseControl
- FuelPump
- PrintToken
- VendingMachine
- DoorController
- INRES protocol
- TCP
- TCSbin(Motorola)





which other lines affect the selected line?



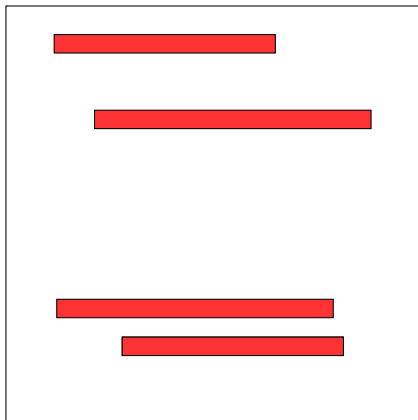
we only care about this line

which other lines affect the selected line?




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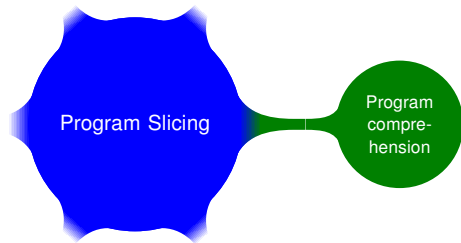
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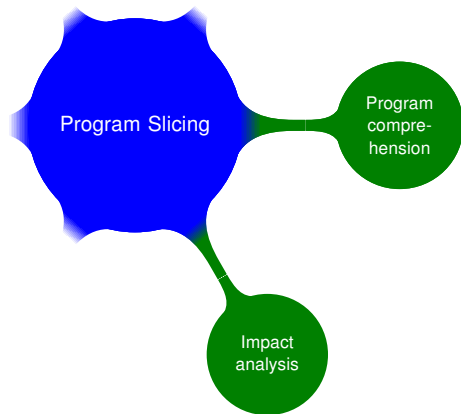
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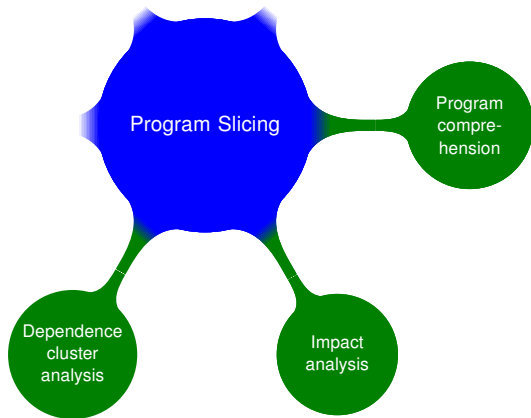


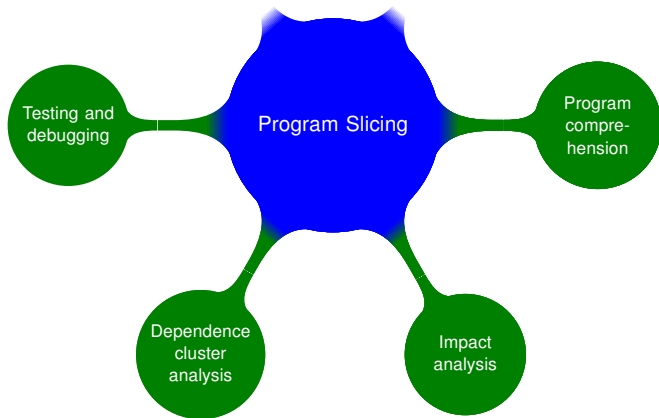
## Program Slicing

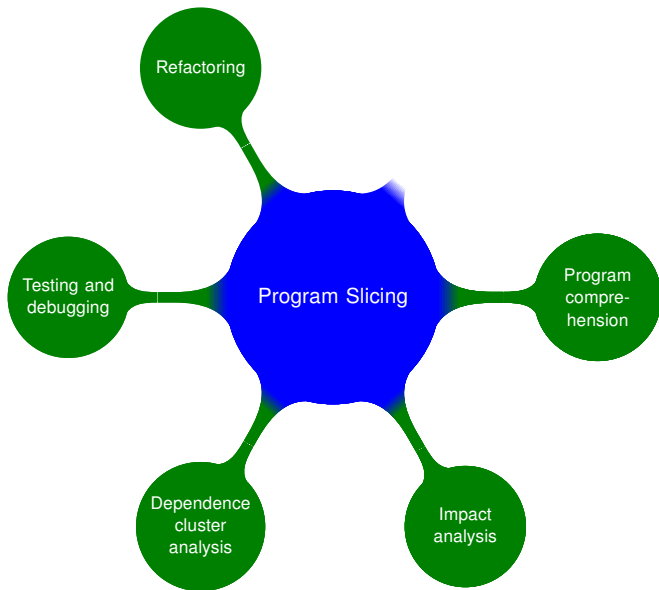






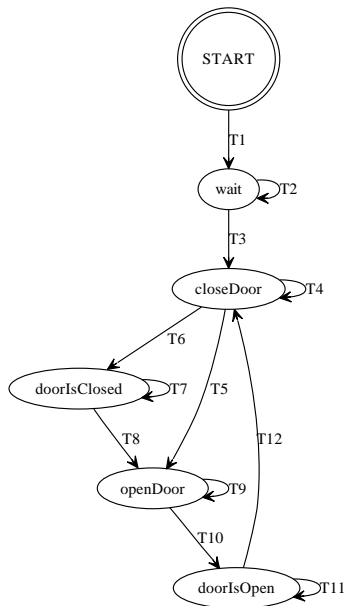


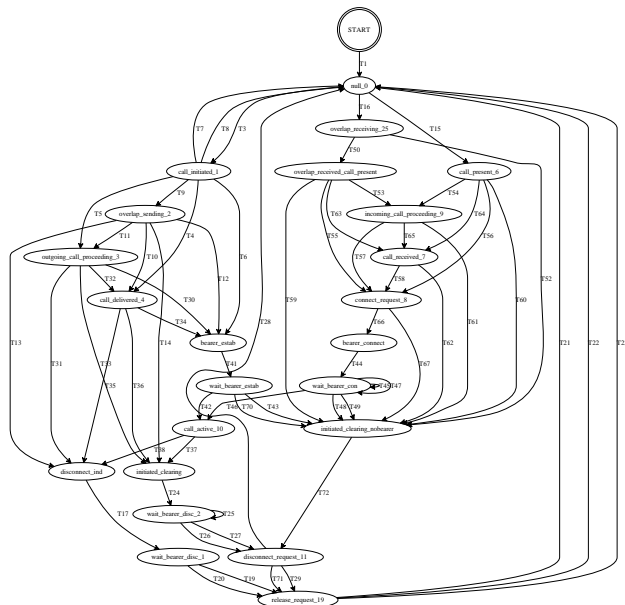






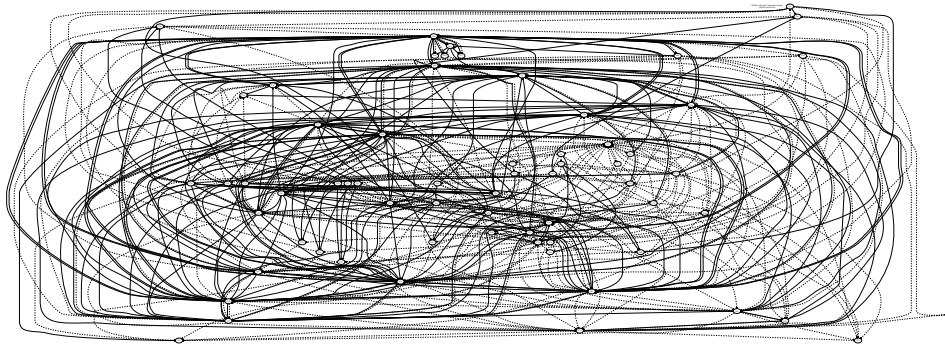
Can slicing be applied to model level?







If the model like this?



## Motivation

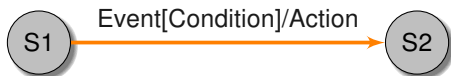
- Models tend to be larger and more complex.

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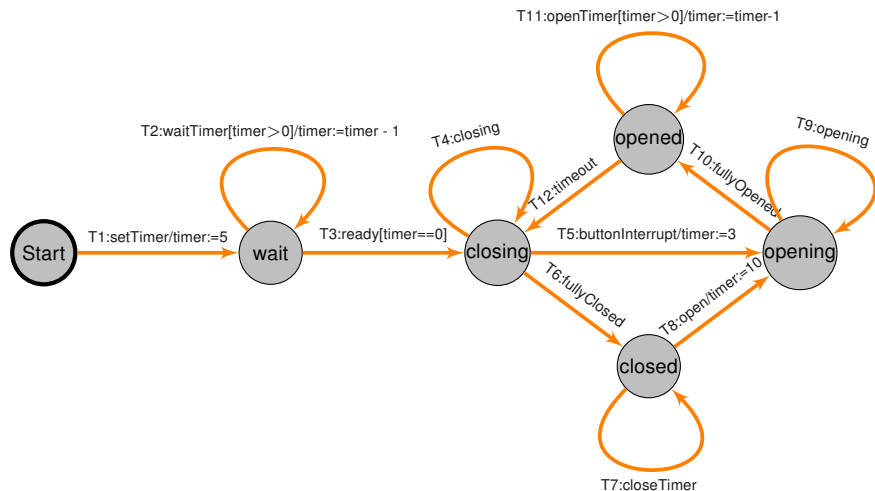
- Models tend to be larger and more complex.
- Slicing has provided a valuable suite of maintenance techniques at the implementation level, but little at model level.

## Definition

An **Extended Finite State Machine (EFSM)**  $M$  is a tuple  $(S, T, E, V)$  where  $S$  is a set of states,  $T$  is a set of transitions,  $E$  is a set of events, and  $V$  is a store represented by a set of variables. Transitions have a source state  $source(t) \in S$ , a target state  $target(t) \in S$  and a label  $lbl(t)$ . Transition labels are of the form  $e_1[c]/a$  where  $e_1 \in E$ ,  $c$  is a condition and  $a$  a sequence of actions.



# An EFSM example: DoorControl



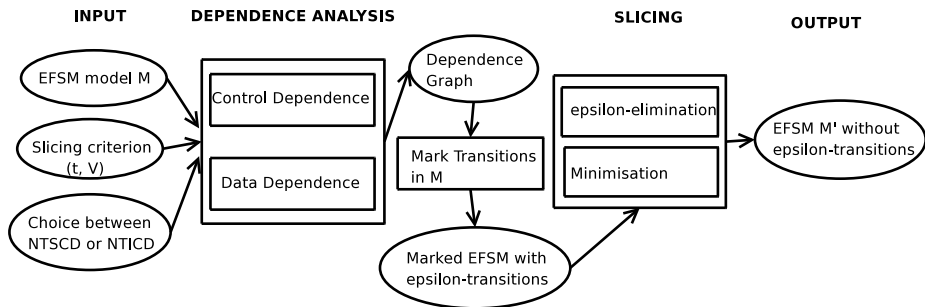
## Definition (Slicing Criterion)

A slicing criterion for an EFSM is a pair  $(t, V)$  where transition  $t \in T$  and variable set  $V \subseteq Var$ . It designates the point in the evaluation immediately after the execution of the action contain in transition  $t$ .

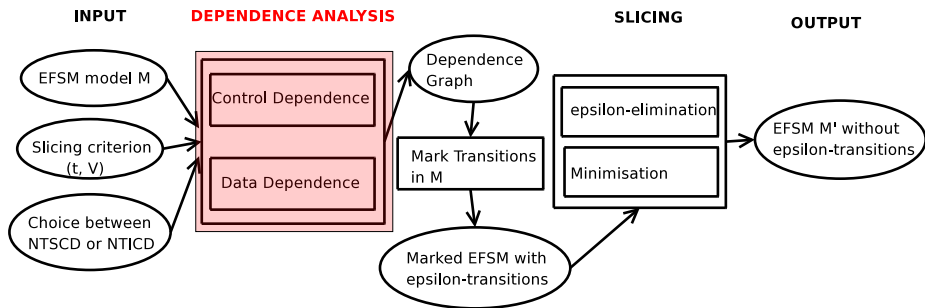
## Definition (Slice)

An EFSM slice  $M'$  is a reduced machine, where for all inputs  $i$  it contains at least one execution where the value of  $v \in V$  at  $t$  is equal to the value of  $v$  at  $t$  in the original EFSM  $M$ .

# The CREST EFSM slicing tool

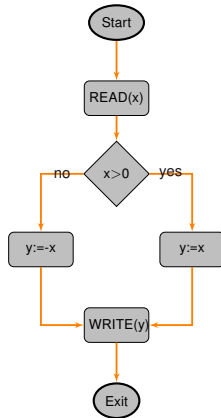
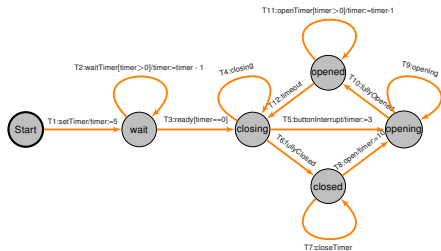


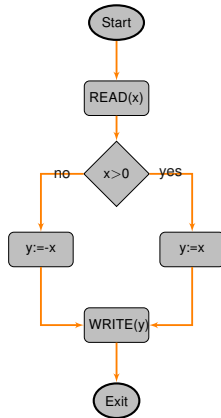
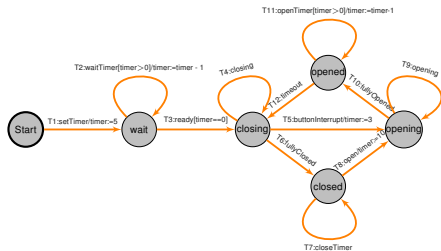
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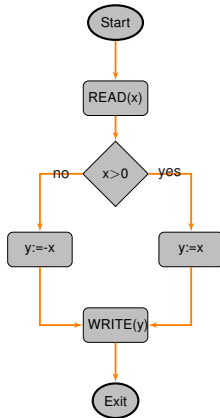
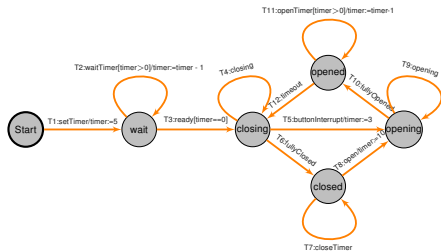
# EFSM VS CFG





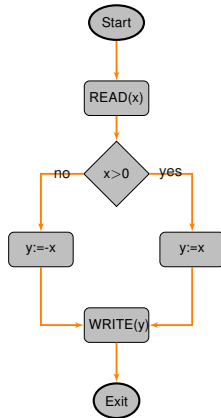
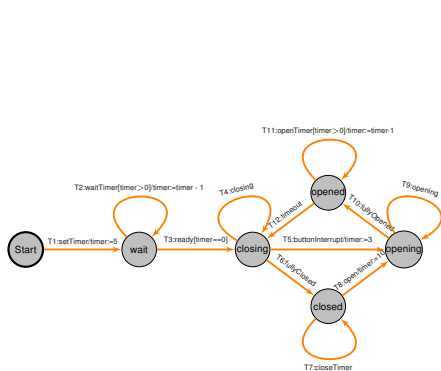
## Difference

- 1 **Transition** in EFSM VS **Node** in CFG



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- 2 Self-looping edge and multi-edges between two nodes



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- 1 **Transition** in EFSM VS **Node** in CFG
- 2 Self-looping edge and multi-edges between two nodes
- 3 Non-termination (Exit node)

- Data Dependence
- Control Dependence

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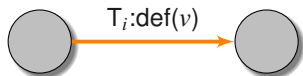
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  - Unfair Non-Termination Insensitive Control Dependence (**UNTICD**) [Androutsopoulos et al. FASE 2009]



## Definition

$T_i \xrightarrow{DD} T_j$  means that transitions  $T_i$  and  $T_j$  are data dependent with respect to a variable  $v$  if:

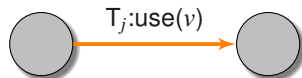
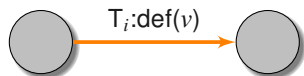
- 1  $v \in D(T_i)$ , where  $D(T_i)$  is a set of variables defined by transition  $T_i$ , i.e. variables defined by actions and by the event of  $T_i$ ;



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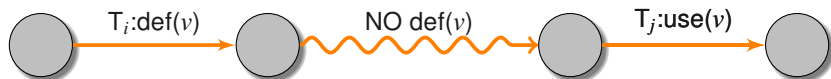
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- 2  $v \in U(T_j)$ , where  $U(T_j)$  is a set of variables used in a condition and actions of transition  $T_j$ ;



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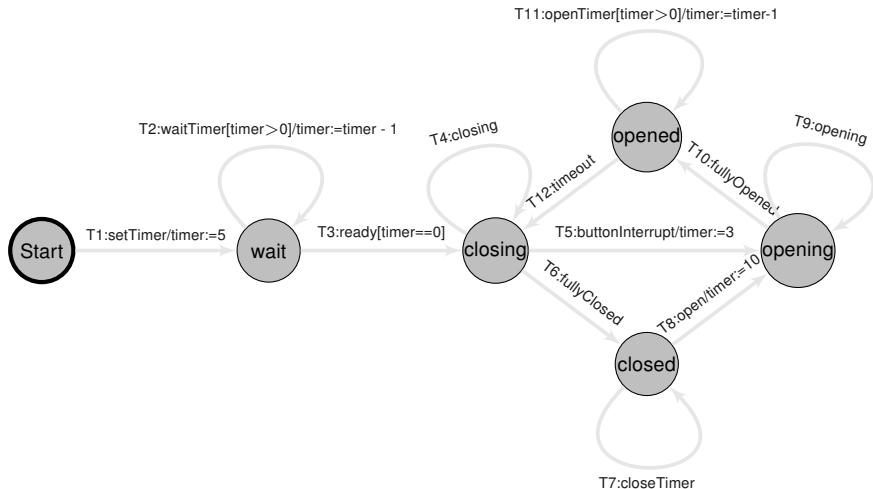
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- 2  $v \in U(T_j)$ , where  $U(T_j)$  is a set of variables used in a condition and actions of transition  $T_j$ ;
- 3 there exists a path in an EFSM from the *source*( $T_i$ ) to the *target*( $T_j$ ) whereby  $v$  is not modified by any of the intermediate transitions.



| <b>Name</b> |   | <b>Path type</b>         |
|-------------|---|--------------------------|
| NTSCD       | → | Maximal Path             |
| NTICD       | → | Sink-bounded Path        |
| UNTICD      | → | Unfair Sink-bounded Path |

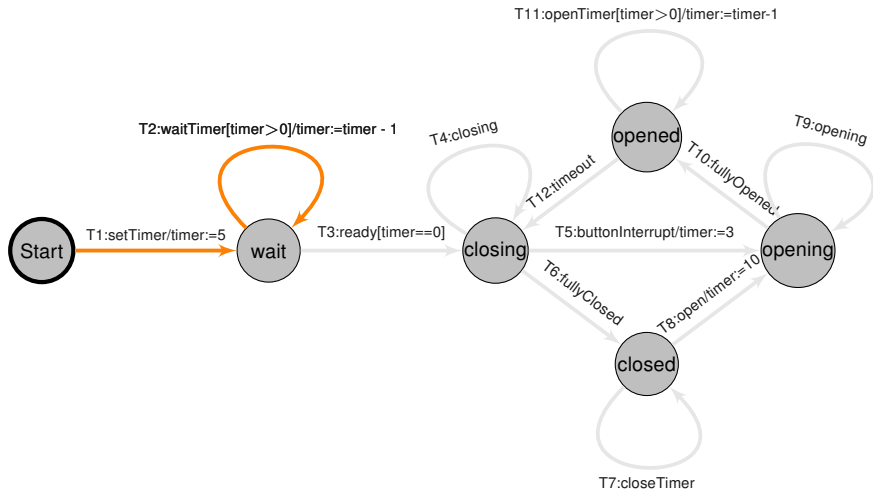
## Definition (Maximal Path)

A **maximal path** is any path that terminates in a final transition, or is infinite.



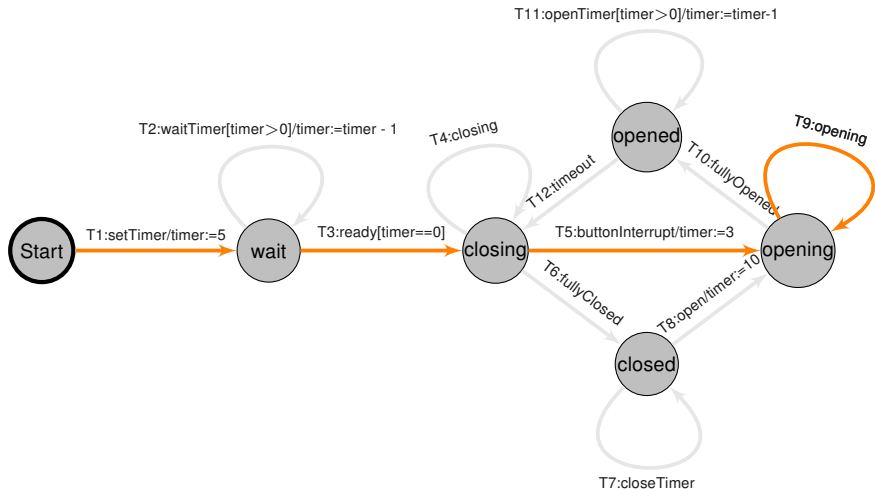
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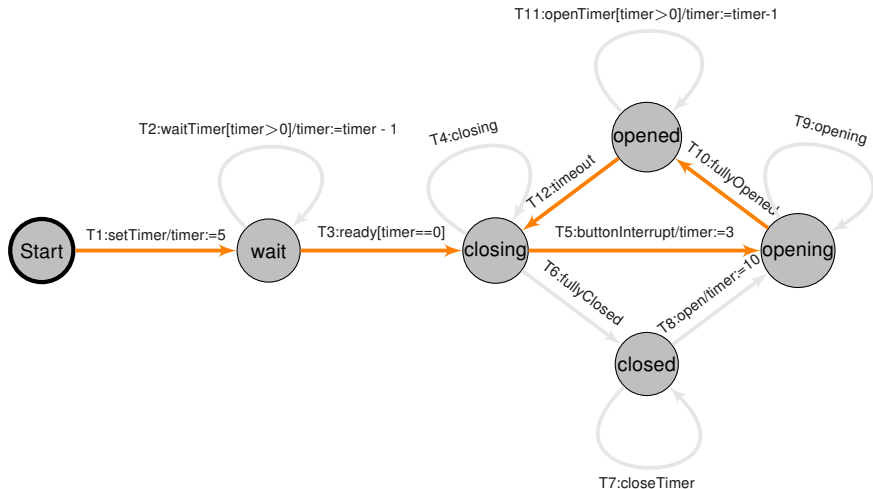
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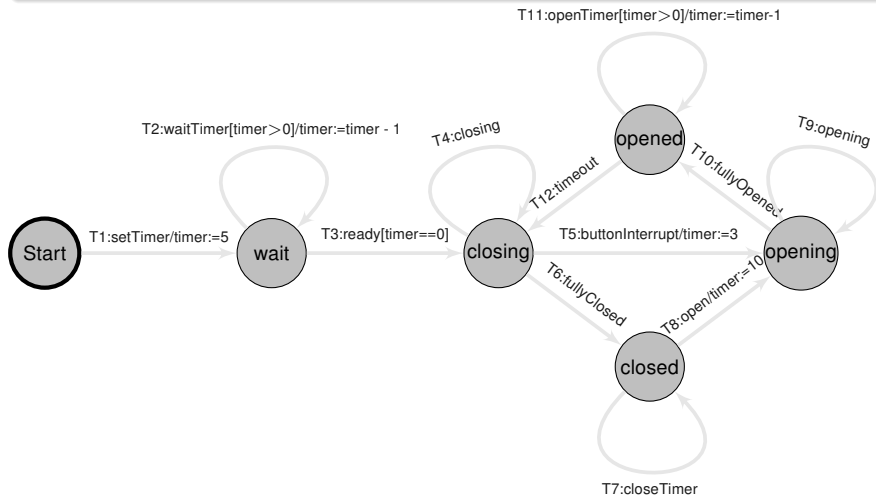
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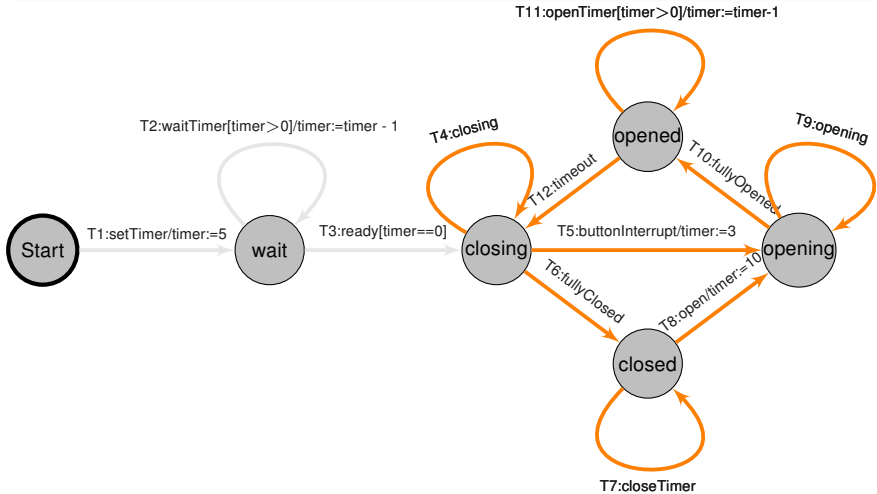
## Definition (Control Sink)

A **control sink** in an EFSM is a set of transitions  $\mathcal{K}$  that form a strongly connected component (SCC) such that, for each transition  $t$  in  $\mathcal{K}$  each successor of  $t$  is also in  $\mathcal{K}$ .



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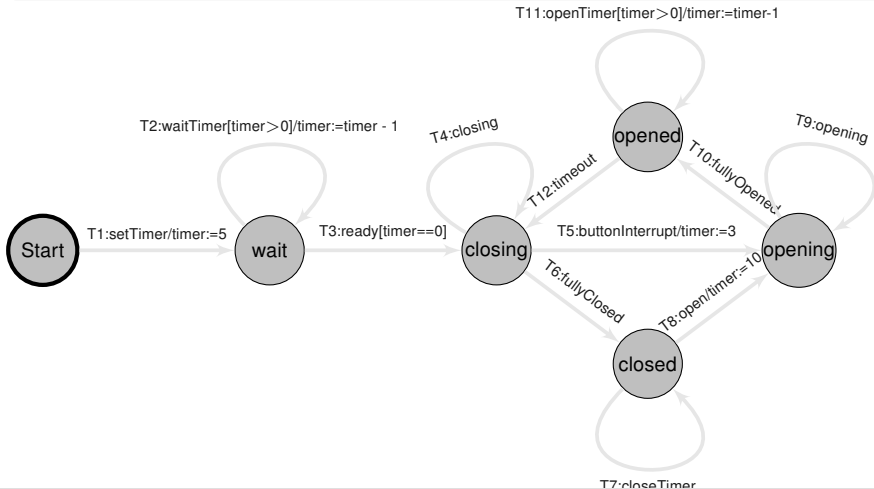
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## Definition (Sink-bounded Paths)

A maximal path  $\pi$  is **sink-bounded** iff there exists a control sink  $\mathcal{K}$  such that:

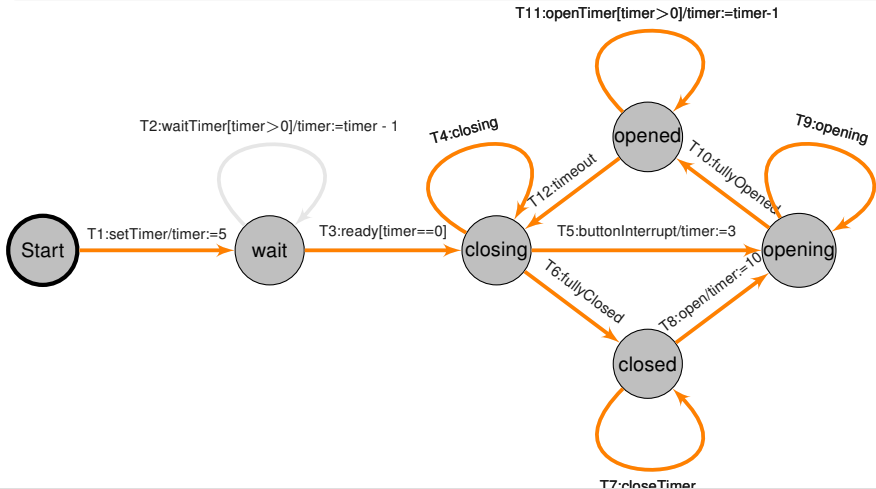
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- if  $\pi$  is infinite, then all transitions in  $\mathcal{K}$  occur infinitely often.



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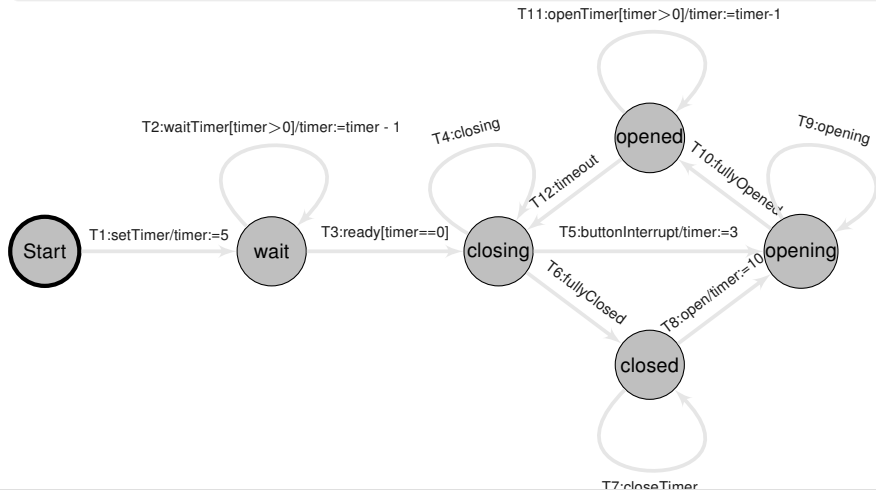
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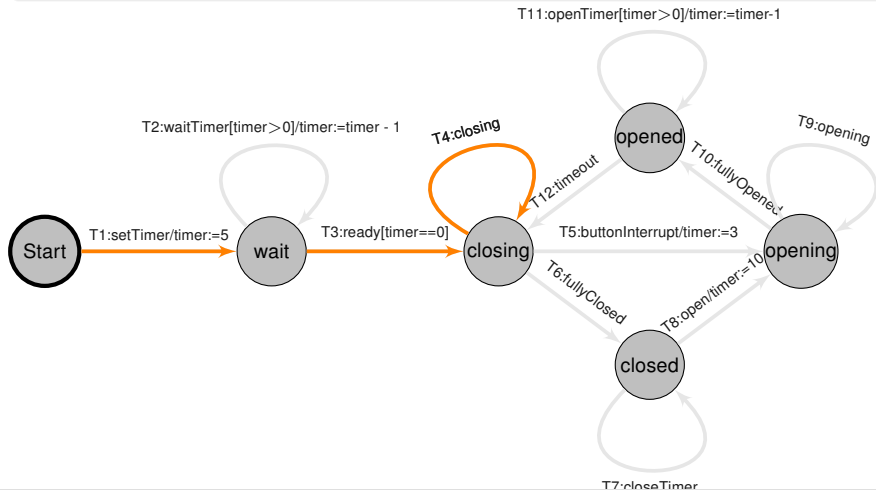
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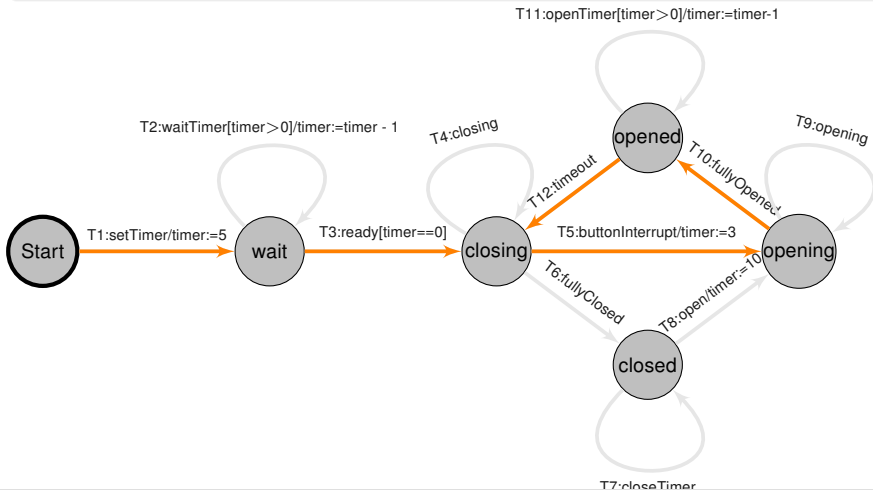
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## Definition (Control Dependence)

$T_i \xrightarrow{\text{CD}} T_j$  means that a transition  $T_j$  is control dependent on a transition  $T_i$  iff  $T_i$  has at least one sibling  $T_k$  such that:

- 1 for all paths  $\pi \in \text{PATHs}(\text{target}(T_i))$ , the  $\text{source}(T_j)$  belongs to  $\pi$ ;
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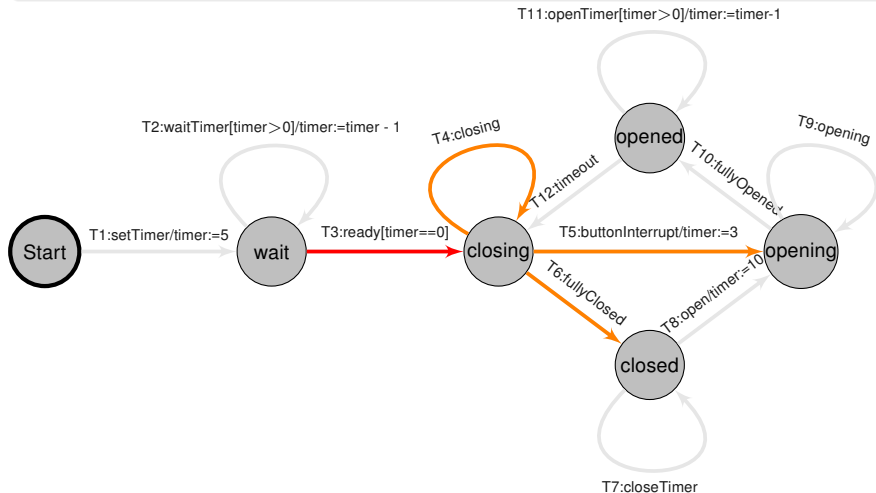
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| CD     |   | PATH type                |
|--------|---|--------------------------|
| NTSCD  | → | Maximal Path             |
| NTICD  | → | Sink-bounded Path        |
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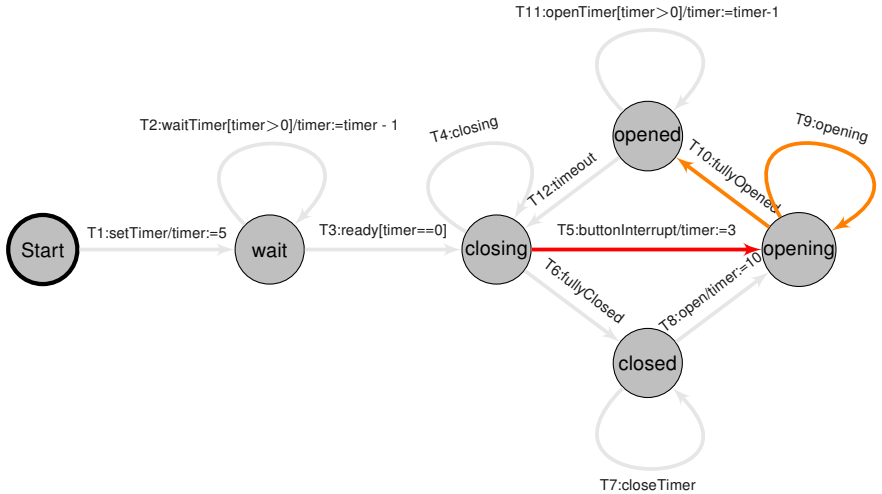
## Example (NTSCD)

- $T_3 \xrightarrow{\text{NTSCD}} T_4, T_5, T_6$
- $T_5 \xrightarrow{\text{NTSCD}} T_9, T_{10}$



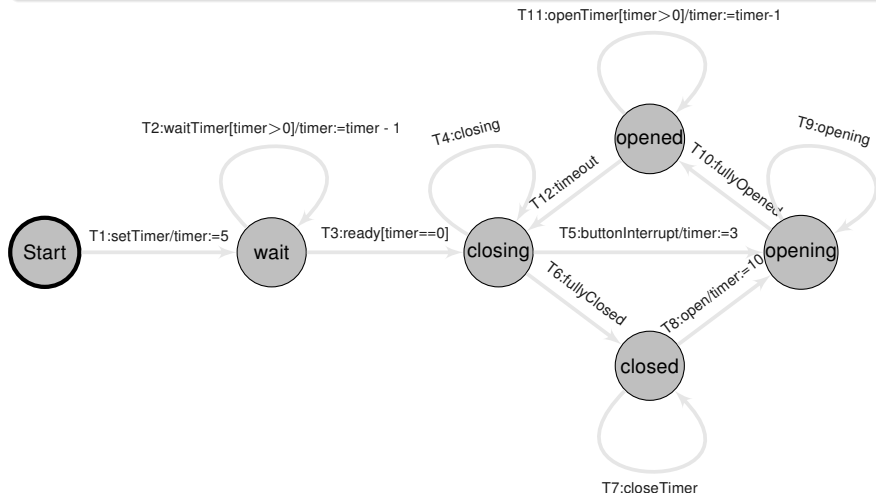
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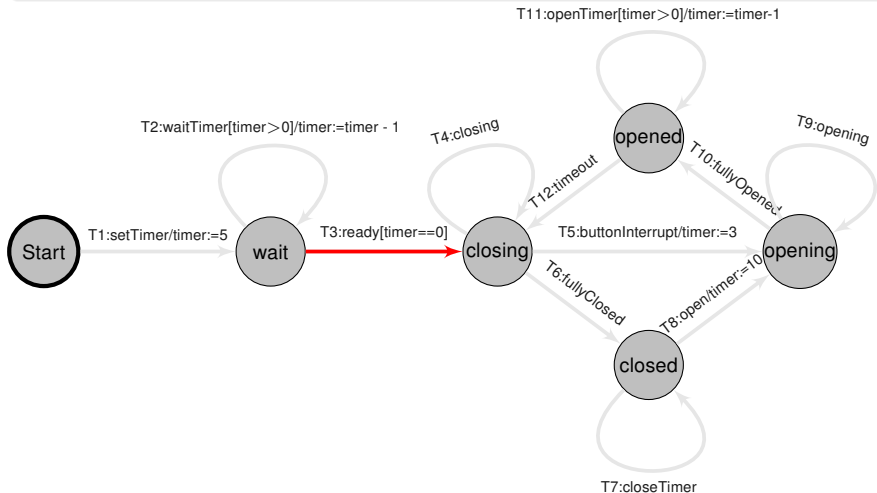
## Example (NTICD)

NO NTICD in this example



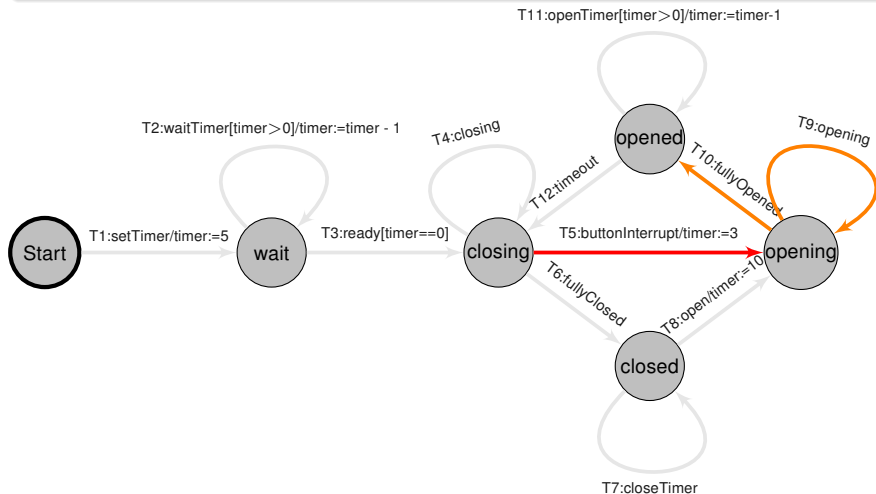
# Example (UNTICD)

- $T_3 \xrightarrow{\text{UNTICD}}$
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- $T_3 \xrightarrow{\text{UNTICD}}$
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## Definition (Slice Size)

For a model  $M$ ,  $t'$  is a transition dependent on  $t$  (i.e.,  $t' \in T \wedge t \rightarrow t'$ ), the size of slice with respect to  $t$  is:

$$|\mathcal{S}(M, t)| = \frac{\sum t'}{|M|}$$

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### Definition (Average Slice Size)

For a model  $M$ ,  $NT$  is subset of transitions of  $M$  with non-zero slice size (i.e.,  $NT \subseteq T$  and  $\forall t \in NT, |\mathcal{S}(M, t)| > 0$ ). Thus, the average slice size of  $M$  is:

$$\text{Avg}(M) = \frac{\sum_{t \in NT} |\mathcal{S}(M, t)|}{|NT|}$$



# Subjects

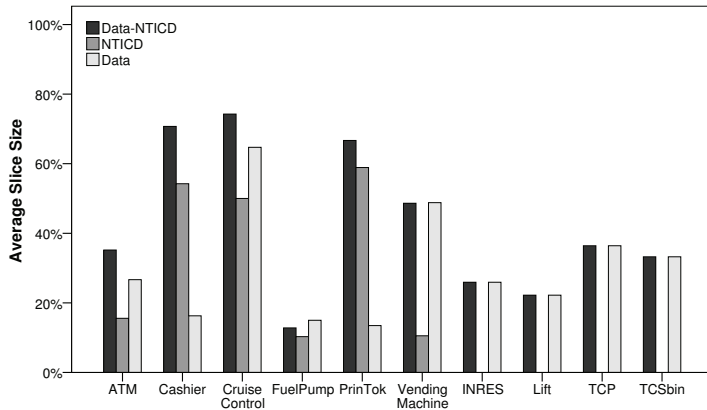
| Models         | #S  | #T  | #V  | EXIT | Description                |
|----------------|-----|-----|-----|------|----------------------------|
| ATM            | 9   | 23  | 8   | Yes  | Automated Teller Machine   |
| Cashier        | 12  | 21  | 10  | Yes  | Cashier Machine            |
| CruiseControl  | 5   | 17  | 18  | Yes  | Cruise Control System      |
| FuelPump       | 13  | 25  | 12  | Yes  | Fuel Pump System           |
| PrinTok        | 11  | 89  | 5   | Yes  | Print Token                |
| VendingMachine | 7   | 28  | 7   | Yes  | Vending Machine system     |
| INRES          | 8   | 18  | 8   | No   | INRES protocol             |
| TCP            | 12  | 57  | 31  | No   | TCP Standard(RFC793)       |
| TCSbin         | 24  | 65  | 61  | No   | Telephony Control Protocol |
| Lift           | 6   | 12  | 1   | No   | Lift System                |
| <b>Total</b>   | 107 | 355 | 161 |      |                            |

| Dependence | Forward Slices |     | Backward Slices |     |
|------------|----------------|-----|-----------------|-----|
|            | # T            | Avg | # T             | Avg |
| DD+NTSCD   |                |     |                 |     |
| DD+NTICD   |                |     |                 |     |
| DD+UNTICD  |                |     |                 |     |
| DD         |                |     |                 |     |
| NTSCD      |                |     |                 |     |
| NTICD      |                |     |                 |     |
| UNTICD     |                |     |                 |     |

| Dependence | Forward Slices |        | Backward Slices |     |
|------------|----------------|--------|-----------------|-----|
|            | # T            | Avg    | # T             | Avg |
| DD+NTSCD   | 276            | 87.45% |                 |     |
| DD+NTICD   | 220            | 61.99% |                 |     |
| DD+UNTICD  | 267            | 83.20% |                 |     |
| DD         | 161            | 35.67% |                 |     |
| NTSCD      | 205            | 86.10% |                 |     |
| NTICD      | 92             | 78.67% |                 |     |
| UNTICD     | 190            | 82.21% |                 |     |

| Dependence | Forward Slices |        | Backward Slices |        |
|------------|----------------|--------|-----------------|--------|
|            | # T            | Avg    | # T             | Avg    |
| DD+NTSCD   | 276            | 87.45% | 345             | 70.46% |
| DD+NTICD   | 220            | 61.99% | 278             | 49.48% |
| DD+UNTICD  | 267            | 83.20% | 335             | 66.83% |
| DD         | 161            | 35.67% | 174             | 33.15% |
| NTSCD      | 205            | 86.10% | 336             | 53.63% |
| NTICD      | 92             | 78.67% | 167             | 44.59% |
| UNTICD     | 190            | 82.21% | 313             | 51.00% |

# Backward Slice size using NTICD



# Correlation of Slice Size

| Model          | Dependence | Forward |        |       | Backward |        |       |
|----------------|------------|---------|--------|-------|----------|--------|-------|
|                |            | NTICD   | UNTICD | NTSCD | NTICD    | UNTICD | NTSCD |
| ATM            | NTICD      | -       | 1.000  | .652  | -        | 1.000  | .941  |
|                | UNTICD     | 1.000   | -      | .652  | 1.000    | -      | .941  |
|                | NTSCD      | .652    | .652   | -     | .941     | .941   | -     |
| Cashier        | NTICD      | -       | 1.000  | .898  | -        | 1.000  | 1.000 |
|                | UNTICD     | 1.000   | -      | .898  | 1.000    | -      | 1.000 |
|                | NTSCD      | .898    | .898   | -     | 1.000    | 1.000  | -     |
| CruiseControl  | NTICD      | -       | 1.000  | 1.000 | -        | 1.000  | 1.000 |
|                | UNTICD     | 1.000   | -      | 1.000 | 1.000    | -      | 1.000 |
|                | NTSCD      | 1.000   | 1.000  | -     | 1.000    | 1.000  | -     |
| FuelPump       | NTICD      | -       | 1.000  | .786  | -        | 1.000  | -.509 |
|                | UNTICD     | 1.000   | -      | .786  | 1.000    | -      | -.509 |
|                | NTSCD      | .786    | .786   | -     | -.509    | -.509  | -     |
| PrinTok        | NTICD      | -       | 1.000  | 1.000 | -        | 1.000  | 1.000 |
|                | UNTICD     | 1.000   | -      | 1.000 | 1.000    | -      | 1.000 |
|                | NTSCD      | 1.000   | 1.000  | -     | 1.000    | 1.000  | -     |
| VendingMachine | NTICD      | -       | 1.000  | .360  | -        | 1.000  | .224  |
|                | UNTICD     | 1.000   | -      | .360  | 1.000    | -      | .224  |
|                | NTSCD      | .360    | .360   | -     | .224     | .224   | -     |
| INRES          | NTICD      | -       | x      | x     | -        | x      | x     |
|                | UNTICD     | x       | -      | 1.000 | x        | -      | 1.000 |
|                | NTSCD      | x       | 1.000  | -     | x        | 1.000  | -     |
| Lift           | NTICD      | -       | x      | x     | -        | x      | x     |
|                | UNTICD     | x       | -      | .813  | x        | -      | 1.000 |
|                | NTSCD      | x       | .813   | -     | x        | 1.000  | -     |
| TCP            | NTICD      | -       | x      | x     | -        | x      | x     |
|                | UNTICD     | x       | -      | 1.000 | x        | -      | 1.000 |
|                | NTSCD      | x       | .      | -     | x        | 1.000  | -     |
| TCSbin         | NTICD      | -       | x      | x     | -        | x      | x     |
|                | UNTICD     | x       | -      | 1.000 | x        | -      | 1.000 |
|                | NTSCD      | x       | 1.000  | -     | x        | 1.000  | -     |

# Correlation of Slice Size

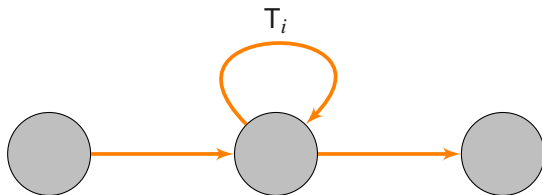
| Model          | Dependence | Forward |        |       | Backward |        |       |
|----------------|------------|---------|--------|-------|----------|--------|-------|
|                |            | NTICD   | UNTICD | NTSCD | NTICD    | UNTICD | NTSCD |
| ATM            | NTICD      | -       | 1.000  | .652  | -        | 1.000  | .941  |
|                | UNTICD     | 1.000   | -      | .652  | 1.000    | -      | .941  |
|                | NTSCD      | .652    | .652   | -     | .941     | .941   | -     |
| Cashier        | NTICD      | -       | 1.000  | .898  | -        | 1.000  | 1.000 |
|                | UNTICD     | 1.000   | -      | .898  | 1.000    | -      | 1.000 |
|                | NTSCD      | .898    | .898   | -     | 1.000    | 1.000  | -     |
| CruiseControl  | NTICD      | -       | 1.000  | 1.000 | -        | 1.000  | 1.000 |
|                | UNTICD     | 1.000   | -      | 1.000 | 1.000    | -      | 1.000 |
|                | NTSCD      | 1.000   | 1.000  | -     | 1.000    | 1.000  | -     |
| FuelPump       | NTICD      | -       | 1.000  | .786  | -        | 1.000  | -.509 |
|                | UNTICD     | 1.000   | -      | .786  | 1.000    | -      | -.509 |
|                | NTSCD      | .786    | .786   | -     | -.509    | -.509  | -     |
| PrinTok        | NTICD      | -       | 1.000  | 1.000 | -        | 1.000  | 1.000 |
|                | UNTICD     | 1.000   | -      | 1.000 | 1.000    | -      | 1.000 |
|                | NTSCD      | 1.000   | 1.000  | -     | 1.000    | 1.000  | -     |
| VendingMachine | NTICD      | -       | 1.000  | .360  | -        | 1.000  | .224  |
|                | UNTICD     | 1.000   | -      | .360  | 1.000    | -      | .224  |
|                | NTSCD      | .360    | .360   | -     | .224     | .224   | -     |
| INRES          | NTICD      | -       | x      | x     | -        | x      | x     |
|                | UNTICD     | x       | -      | 1.000 | x        | -      | 1.000 |
|                | NTSCD      | x       | 1.000  | -     | x        | 1.000  | -     |
| Lift           | NTICD      | -       | x      | x     | -        | x      | x     |
|                | UNTICD     | x       | -      | .813  | x        | -      | 1.000 |
|                | NTSCD      | x       | .813   | -     | x        | 1.000  | -     |
| TCP            | NTICD      | -       | x      | x     | -        | x      | x     |
|                | UNTICD     | x       | -      | 1.000 | x        | -      | 1.000 |
|                | NTSCD      | x       | .      | -     | x        | 1.000  | -     |
| TCSbin         | NTICD      | -       | x      | x     | -        | x      | x     |
|                | UNTICD     | x       | -      | 1.000 | x        | -      | 1.000 |
|                | NTSCD      | x       | 1.000  | -     | x        | 1.000  | -     |

- UNTICD and NTSCD dependences for all transitions within control sinks are identical.
- UNTICD and NTICD dependences for all transitions outside of control sinks are identical.
- The transitive closure for NTICD is contained in the transitive closure for UNTICD.



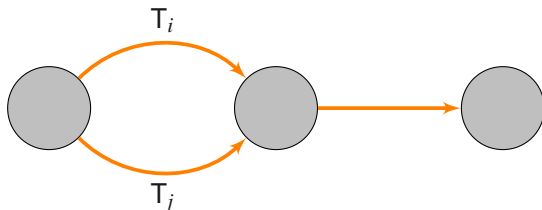
## Proposition

For an EFSM  $M$ , if  $T_i \in M$  is a self-looping transition, then there is no transition  $T_j$  that is control dependent (NTSCD, NTICD or UNTICD) on  $T_i$ .



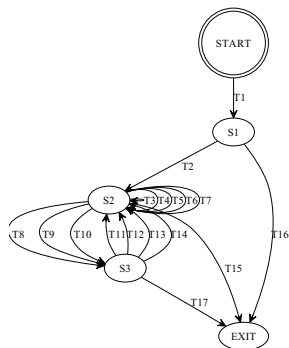
## Proposition

For an EFSM  $M$ , if two transitions  $T_i$  and  $T_j$  have the same source and target states, and  $T_i \xrightarrow{CD} T_l$  (using NTSCD, NTICD or UNTICD) then  $T_j \xrightarrow{CD} T_l$  (using NTSCD, NTICD or UNTICD respectively).



## Proposition

For an EFSM  $M$ , if all states  $s \in M$  where  $s \neq \text{START}$  have a transition  $T_i$  where  $\text{source}(T_i) = s$  and  $\text{target}(T_i) = \text{EXIT}$ , then the set of transitions that are directly control dependent on  $T_i$  are the same for all types of control dependence, i.e. NTSCD, NTICD and UNTICD.



- NTSCD, NTICD and UNTICD are defined for EFSM
- The properties are formally proved
- Empirically studies on dependence size

# Questions?

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